

# Best Practices for Modeling Time-Varying Selectivity

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# Outline

- 1 Motivation
- 2 Virtual & Synthetic methods
- 3 Selectivity Models
- 4 Simulation Experiment
  - Model overview
  - Simulation results
- 5 Discussion

# Motivation

There are many **SUBJECTIVE** elements in stock assessment.

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# VPA vs. SCA

- **Virtual Population Analysis**
  - ▶ Catch reported without error
  
- **Statistic Catch Age**

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- **Statistic Catch Age**
  - ▶ Confounding between error & structural assumptions



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- Statistic Catch Age
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  - ▶ Separability (year & age effect)

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  - ▶ Catch reported without error
  - ▶ Incomplete cohorts
  - ▶ Error propagation
  
- Statistic Catch Age
  - ▶ Confounding between error & structural assumptions
  - ▶ Seprability (year & age effect)
  - ▶ Large number of latent variables

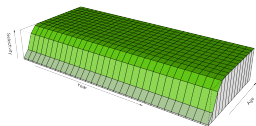
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# Selectivity Models

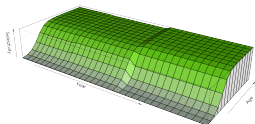
## Fixed

Hake(20) Gear 2



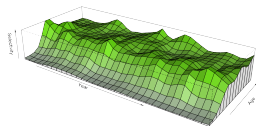
## Discrete

Hake(20) Gear 1



## Continuous

Hake(20) Gear 1



Asymptotic or dome?

Choice of time blocks?

Variance on penalty?

*How do we go about choosing the appropriate model?*

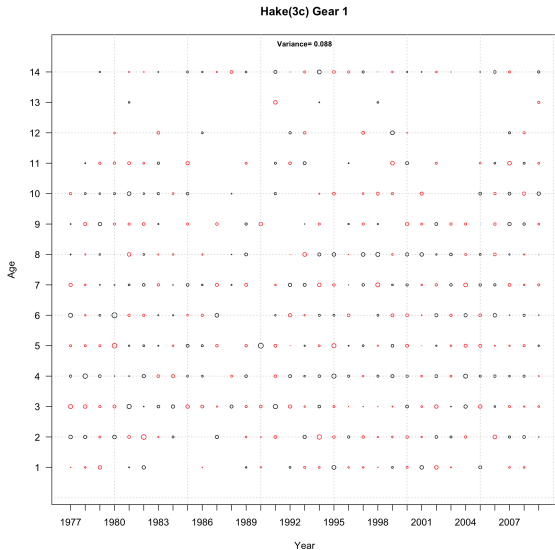
# How do we go about choosing the appropriate model?

*Fishing epochs*



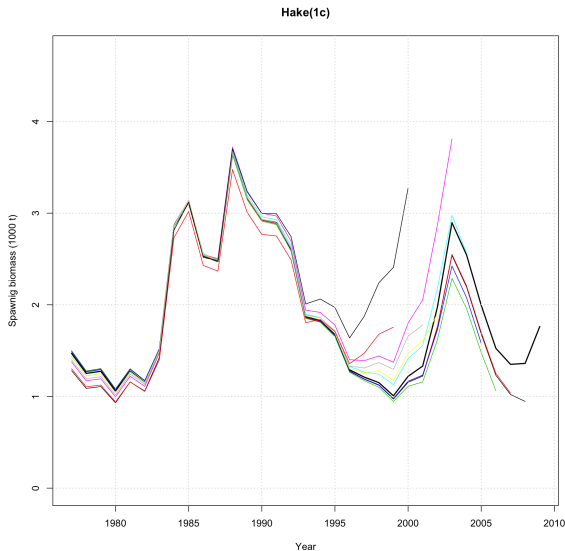
# How do we go about choosing the appropriate model?

## *Residual patterns*



# How do we go about choosing the appropriate model?

## *Retrospective performance*



How do we go about choosing the appropriate model?

Center for Independent Experts!



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## Simulation experiment

<u>True states</u>	<u>Assumed selectivity states</u>		
	<b>Fixed (a)</b> <b>N=89</b>	<b>Discrete (b)</b> <b>N=93</b>	<b>Continuous (c)</b> <b>N=318</b>
<b>Fixed (1)</b>	1a	1b	1c
<b>Discrete (2)</b>	2a	2b	2c
<b>Continuous (3)</b>	3a	3b	3c

## Model structure

Simulation: based on 2010 Pacific hake assessment

- Age-structured, assume  $M$  is known.
- Conditioned on historical catch & parameters fixed at MLE values.
- Parameters:  $B_0$ ,  $h$ , initial states, rec-devs, selectivities,  $F$ 's,  $q$ , total variance.
- Concentrated likelihood for age-comps & estimate total variance.

Data:

- Historical removals.
- Annual abundance index based on stationary  $q$ .
- Survey age composition (logistic-time invariant).
- Fishery age composition (selectivity: fixed, blocks, or continuous).
- Index observation error:  $\sigma = 0.40$
- Age-composition error (multivariate logistic):  $\sigma = 0.40$
- Process error:  $\tau = 1.12$

# Questions

- ① Can DIC be used reliably to choose the correct selectivity model?
- ② Impact of selectivity mis-specification on reference points?
- ③ Retrospective performance of selectivity mis-specification?

# Algorithm

For each model scenario:

- 1 Estimate model parameters for 2010 hake assesment.
- 2 Simulate relative abundance and age-comps based on MLE values.
- 3 Estimate joint posterior for simulated observations.
- 4 Calculate DIC from 1000 posterior samples.
- 5 Compute bias in estimated reference points.
- 6 Compute 4-year mean retrospective bias.
- 7 Repeat steps 2:5 at least 100 times for each scenario (9).

## Model Selection

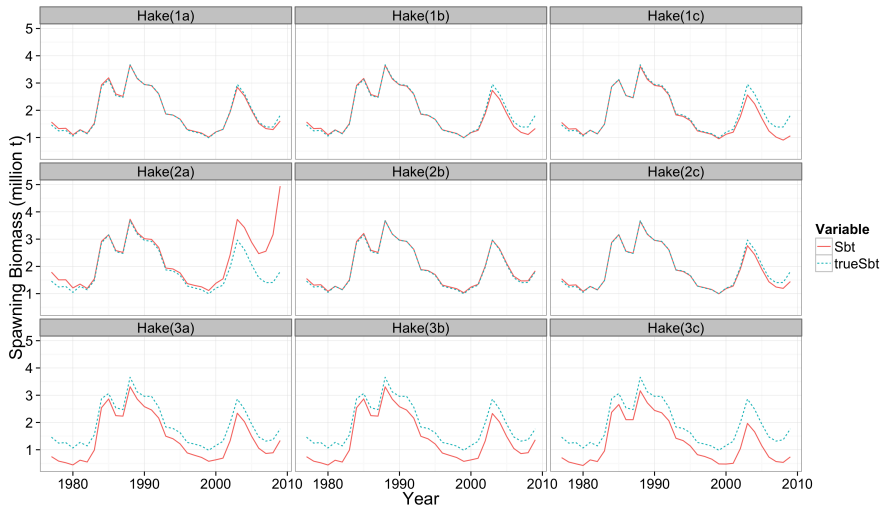
Can DIC be used reliably to choose the correct selectivity model?

DIC based on 1000 samples from the joint posterior.

Monte carlo runs based on 24 simulated data sets per treatment.

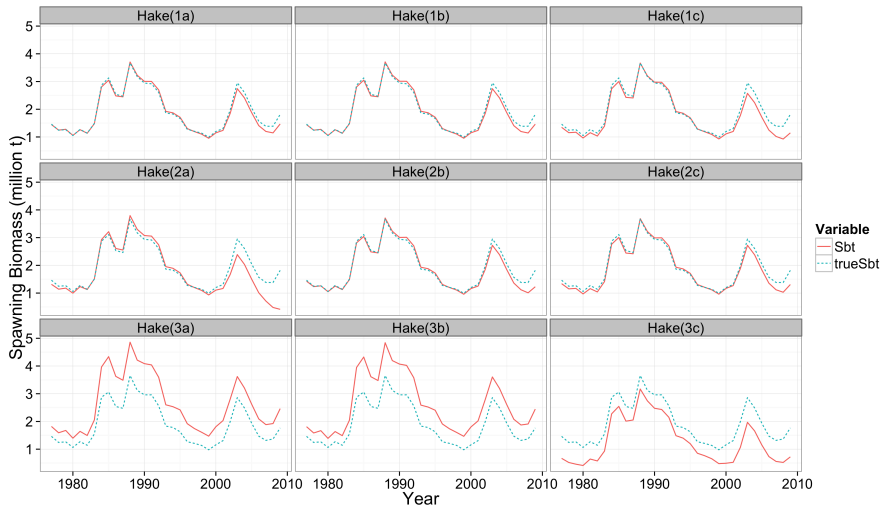
# Spawning biomass

Seed=991



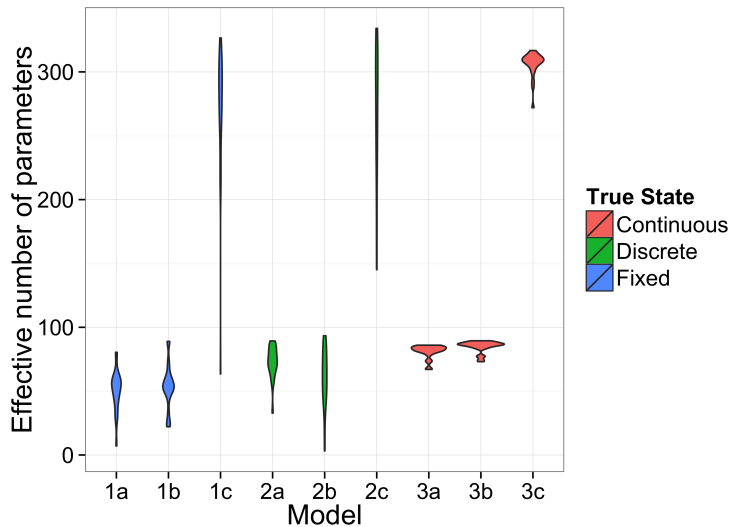
# Spawning biomass

Seed = 123

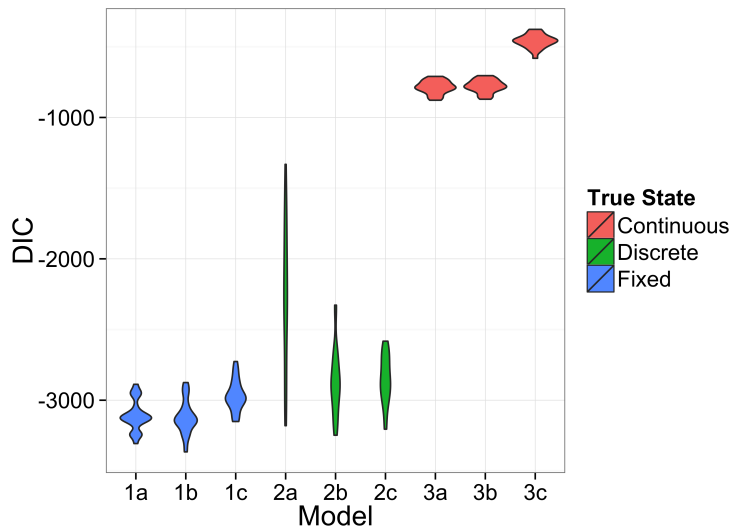




# Effective number of parameters



# Model selection vis-à-vis DIC



## Impacts on reference points

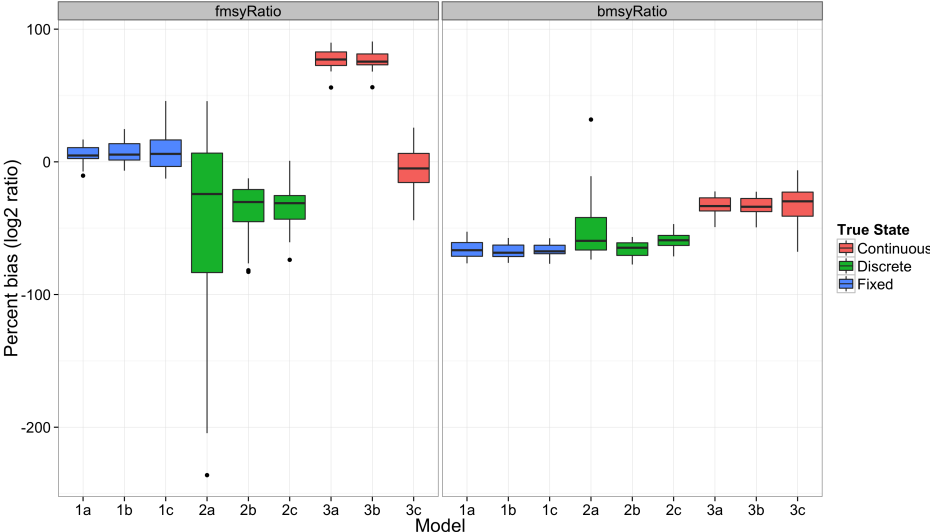
Impact of selectivity mis-specification on reference points?

MSY-based reference points based on MLE estimates.

Monte carlo runs based on 24 simulated data sets per treatment.

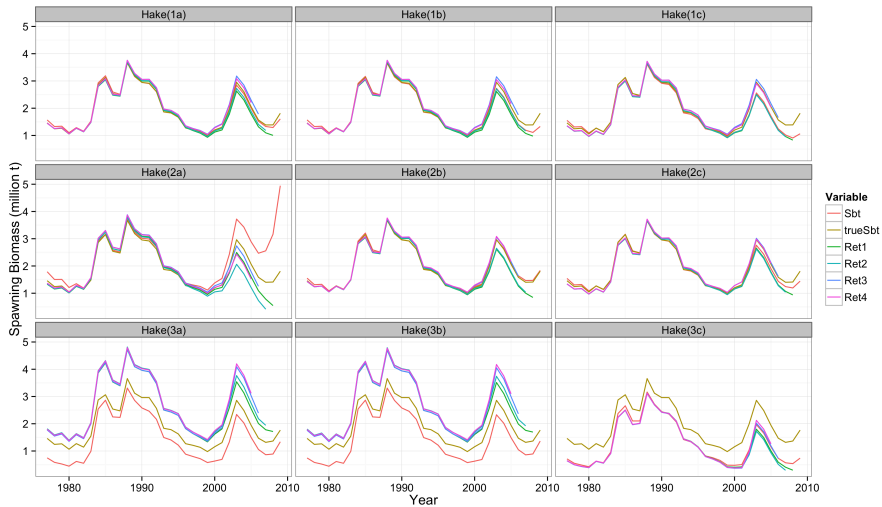
Compute  $\log_2 \left( \frac{F_{est}}{F_{true}} \right)$

# Impacts on reference points



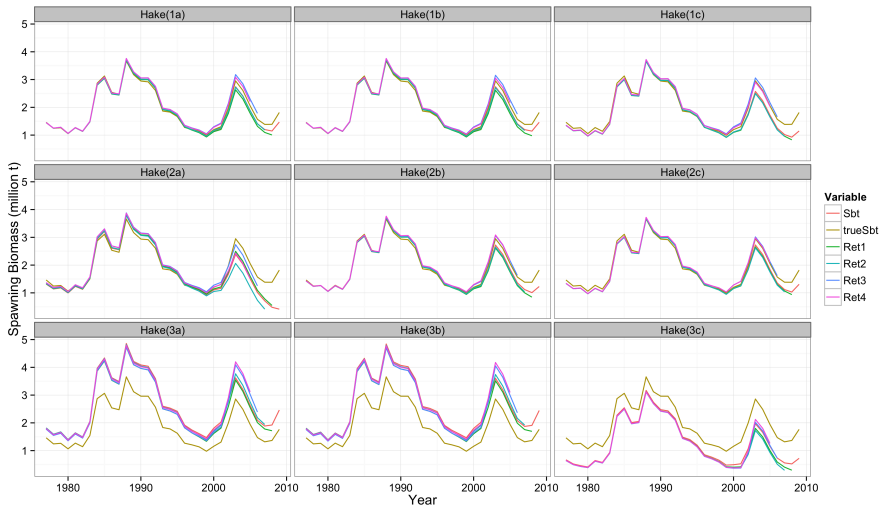
# Retrospective bias

Seed = 991



# Retrospective bias

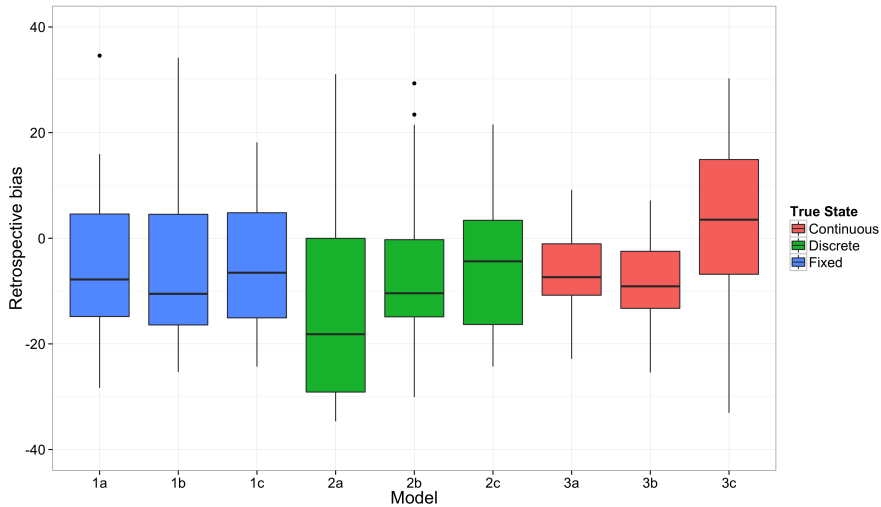
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## Retrospective bias

$$\text{bias} = \frac{1}{4} \sum_{t=2005}^{2009} 100 \frac{B_t^y - B_t^{2010}}{B_t^{2010}}$$

# Retrospective bias





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- Preferable to adopt a penalized random walk versus time blocks.
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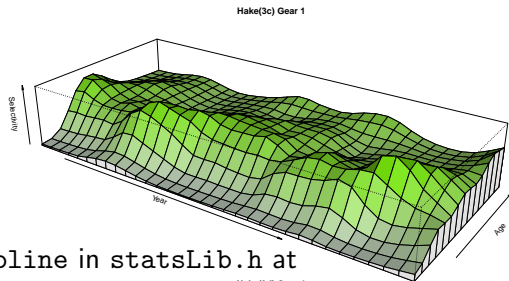
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- And there is one more thing....
  - ▶ Can also use 2 dimensional splines for selectivity.

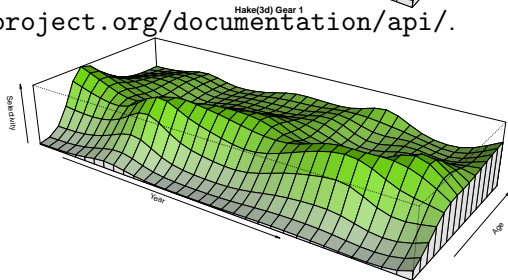


## 2d cubic splines

Top = 231 and bottom = 60 selectivity parameters.



See `bicubic_spline` in `statsLib.h` at  
<http://admb-project.org/documentation/api/>.



## The End

### Acknowledgements:

IPHC, ADMB Foundation, CAPAM workshop organizers.

Jim Ianelli and Dave Fournier for the `vcubicspline_function_array` class.